

# Drivers of Concentration: the Roles of Trade Access, Structural Transformation, and Local Fundamentals

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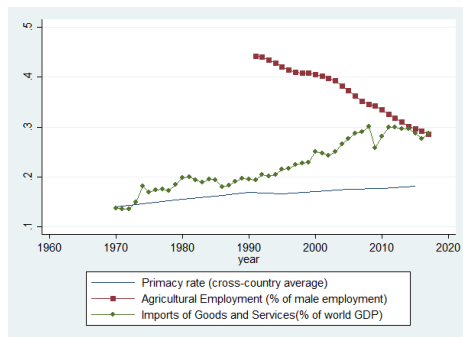
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- **Question:** which factors determine how concentrated in space a country's population is?
- **Importance:**
  - Modern spatial concentration associated with economic development (Glaeser '11).
  - Spatial responses may influence welfare effects of economic shocks.
    - e.g. trade shocks
  - Help predict effects of future events on world's economic geography.
    - Retreat of globalization (e.g. protectionism, pandemics).
    - Developing countries' transition away from agriculture.

# Three Potential Drivers of Concentration

- Location-specific **fundamentals**: productivities and amenities
  - Traditional urban economics (e.g. Rosen-Roback)
- Differential access to **trade networks** (e.g. Redding Sturm 2008)
- **Structural transformation** (e.g. Eckert Peters '18)

- Globally, these factors correlate over time.
  - Spatial concentration metric: *primacy rate*
  - i.e. % of national population living in country's largest location.



- Investigate roles of three drivers of spatial concentration through lens of modern quantitative spatial model (QSM).
- ① Create **theoretical framework** featuring the three drivers:
  - Must add non-homothetic preferences to workhorse QSM.
  - Derive expression decomposing spatial concentration into each driver's contribution.
- ② **Estimate** global **trade-cost** structure (1962-2019).
- ③ **Calibrate** model to world economy (1990, 2005).
  - i.e. find fundamentals that rationalize observed population/income.
  - World has 192 countries comprising 1611 subnational units.
- ④ Use model to perform **counterfactual** exercises:
  - Shock 2005 system with alternative trade-cost structures.
  - *Result*: trade integration *reduces* concentration for most countries.
- ⑤ **Accounting**: % of 1990-2005 concentration changes explained by each driver.
  - *Result*: changes in fundamentals account for 99% of variation.
  - Trade access and structural change play minor roles.

- Access to Trade Networks:
  - Redding Sturm '08, Ahlfeldt et al '14, Donaldson Hornbeck '16, Brulhart et al '19
- Structural transformation:
  - Boppart '14, Eckert Peters '18
- New Economic Geography (NEG):
  - Krugman Livas '96, Ades Glaeser '95, Krugman '91, Krugman Venables '95
- International trade and countries' internal structure:
  - Fajgelbaum Redding '14, Cosar Fajgelbaum '16, ECLAC '05
- Gravity trade models:
  - Anderson van Wincoop '03, Head Mayer '14, Santos-Silva Terneyro '06
- Quantitative spatial models:
  - Allen Arkolakis '14, Allen Donaldson '20, Caliendo et al '18, Desmet et al '18, Ramondo et al '12 '16, Redding '16, Adao et al '20

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# Model: Overview

- QSM (Allen Arkolakis '14, Allen Donaldson '22), applied to international context:
  - Many countries, partitioned into locations (e.g. states, provinces). Setting
- Non-homothetic preferences over two sectors (agriculture vs rest):
  - Price-Independent Generalized Linear (PIGL) form. PIGL
  - Structural transformation: agriculture to non-agriculture.
- Agents can migrate across domestic locations (but not internationally).
  - Decision considers real wages, amenities, idiosyncratic preference shocks. Migration
- Other assumptions are conventional:
  - Within-sector CES preferences for geographically differentiated goods (Armington).
  - Perfectly competitive firm only use labor input, incur “iceberg” trade costs. Firm
  - External economies of scale (i.e. agglomeration economies).
  - Local amenities are subject to congestion.
  - Heterogeneity in local fundamentals (productivities/amenities).
- Given assumptions, trade/migration flows take a “gravity” form. Gravity



# Model: Equilibrium System

- Equilibrium determined by a system of equations:

$$w_i^{\sigma_s} (L_i^s)^{1-\alpha_s(\sigma_s-1)} = (\bar{A}_i^s)^{\sigma_s-1} \sum_{j \in \mathcal{S}} (\tau_{ij}^s)^{1-\sigma_s} (P_j^s)^{\sigma_s-1} v_j^s L_j w_j \quad (1)$$

$$(P_j^s)^{1-\sigma_s} = \sum_{i \in \mathcal{S}} (\tau_{ij}^s w_i)^{1-\sigma_s} (\bar{A}_i^s (L_i^s)^{\alpha_s})^{\sigma_s-1} \quad (2)$$

$$L_i^A + L_i^N = L_i = \frac{W_i^\theta}{\sum_{k \in \mathcal{C}} W_k^\theta} \bar{L}_c \quad (3)$$

$$W_j = \bar{u}_j L_j^\beta \left[ \frac{1}{\eta} (w_j (P_j^A)^{-\phi} (P_j^N)^{\phi-1})^\eta - \frac{\nu}{\gamma} (P_j^A / P_j^N)^\gamma + \frac{\nu}{\gamma} - \frac{1}{\eta} \right] \quad (4)$$

- Equilibrium:** set of endogenous variables ( $w$ ,  $L$ ,  $L^s$ ,  $W$ ,  $P^s$ ,  $v^s$ ) that satisfies equations (1)-(4) given parameters ( $\sigma_s$ ,  $\theta$ ,  $\alpha_s$ ,  $\beta$ ,  $\nu$ ,  $\eta$ ,  $\gamma$ ) and exogenous variables  $(\bar{A}^s, \bar{u})$ ,  $(\tau^s)$ ,  $\{\bar{L}_c\}_{c \in \mathcal{C}}$ . Equilibrium Conditions

- Under parametric assumptions ( $\sigma_s = \sigma$ ,  $\alpha_s = \alpha$ ) primacy rate is:

$$Primacy_c \equiv \frac{L_{p(c)}}{\bar{L}_c} = \frac{\left( \bar{u}_{p(c)} \rho_{p(c)} \zeta_{p(c)}^{-\frac{\eta}{\Omega}} \right)^{\frac{\theta}{1-\theta(\beta+\eta/\Omega)}}}{\sum_{k \in c} \left( \bar{u}_k \rho_k \zeta_k^{-\frac{\eta}{\Omega}} \right)^{\frac{\theta}{1-\theta(\beta+\eta/\Omega)}}} \quad (5)$$

where:

- $L$  is population, and  $p(c)$  is primate location of country  $c$
  - $\bar{u}$  is fundamental amenity,  $\bar{A}$  is fundamental productivity,  $v^A$  is agricultural expenditure share
  - $\rho_i = \frac{1}{\eta} (P_i^A)^{-\eta\phi} (P_i^M)^{\eta(\phi-1)} - \frac{1}{\gamma} (v_i^A - \phi)$  is consumer trade access
  - $\Pi_i^S = \sum_{j \in S} (\tau_{ij}^S)^{1-\sigma} (P_j^S)^{\sigma-1} v_j^S w_j L_j$  is producer trade access
  - $\zeta_i = \sum_s [(\bar{A}_i^S)^{\sigma-1} \Pi_i^S]^{\frac{1}{1-\alpha(\sigma-1)}}$
  - $\Omega \equiv \sigma / (\alpha(\sigma-1) - 1)$
- Intuition:** primacy increasing in primate's fundamentals (productivities and amenities) and trade access relative to other domestic locations.

# Model: Primacy Rate (Differential Version)

- This differential version will later be brought to the data (“change accounting”):

$$\left( \frac{1 - \theta(\beta + \frac{\eta}{\Omega})}{\theta} \right) d \ln(\text{Primacy}_c) = \text{contrib}_c^{ST} + \text{contrib}_c^{DTA} + \text{contrib}_c^{LF} \quad (6)$$

where:

$$\begin{aligned} \text{contrib}_c^{ST} &= \underbrace{\kappa_{p(c)}(-dv_{p(c)}^A) - \sum_{k \in c} \left( \frac{L_k}{L_c} \right) \kappa_k(-dv_k^A)}_{\text{Structural Transformation}} \\ \text{contrib}_c^{DTA} &= \underbrace{\left[ \Gamma_{p(c)} d \ln(I_{p(c)}) - \sum_{k \in c} \left( \frac{L_k}{L_c} \right) \Gamma_k d \ln(I_k) \right]}_{\text{Differential Trade Access \#1: Consumer Trade Access}} + \underbrace{\frac{\eta}{\sigma} \left[ \sum_s \mu_{p(c)}^s d \ln(\Pi_{p(c)}^s) - \sum_{k \in c} \left( \frac{L_k}{L_c} \right) \sum_s \mu_k^s d \ln(\Pi_k^s) \right]}_{\text{Differential Trade Access \#2: Producer Trade Access}} \\ \text{contrib}_c^{LF} &= \underbrace{\left[ d \ln(\bar{u}_{p(c)}) - \sum_{k \in c} \left( \frac{L_k}{L_c} \right) d \ln(\bar{u}_k) \right]}_{\text{Local Fundamental \#1: Amenities}} + \underbrace{\frac{\eta(\sigma - 1)}{\sigma} \left[ \sum_s \mu_{p(c)}^s d \ln(\bar{A}_{p(c)}^s) - \sum_{k \in c} \left( \frac{L_k}{L_c} \right) \sum_s \mu_k^s d \ln(\bar{A}_k^s) \right]}_{\text{Local Fundamental \#2: Sectoral Productivities}} \end{aligned}$$

$$\text{and: } \mu_i^s \equiv (\zeta_i)^{-1} [(\bar{A}_i^s)^{\sigma-1} \Pi_i^s]^{-\frac{1}{1-\alpha(\sigma-1)}}, \quad l_i = (P_i^A)^{-\phi} (P_i^N)^{\phi-1}, \quad \kappa_i = \frac{1}{\gamma \rho_i}, \quad \Gamma_i = \frac{l_i \eta}{\rho_i}$$

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# Estimating Trade Costs

- To bring model to the data, first step is to estimate global trade costs.
- Impose functional form for trade costs (Ramondo et al '14):

$$\tau_{ijt}^s = (E_t^s)^{\mathbb{1}_{j \notin c(i)}} \prod_{z=1}^B (C^{s,z})^{\mathbb{1}_{dist_{ij} \in b_z}}$$

- $E_t^s$ : border-crossing parameter
- $\{b_z\}_{z=1}^B$ : set of distance “bins” Computing distances
- In consequence, the model's gravity trade equation becomes estimable:

$$\ln(X_{ijt}^s) = \sum_{z=1}^B \underbrace{(1 - \sigma_s) \ln(C^{s,z})}_{\check{c}^{s,z}} \mathbb{1}_{dist_{ij} \in b_z} + \underbrace{(1 - \sigma_s) \ln(E_t^s)}_{\check{E}_t^s} \mathbb{1}_{j \notin c(i)} + \omega_{it}^{s,X} + \omega_{jt}^{s,M} + \eta_{ijt}^s \quad (7)$$

## Results: Trade Costs (1/2)

- Estimate gravity trade equation (7) using PPML (Santos-Silva Tenreyro '06)
  - Recover  $\{\hat{E}_t^s, \hat{C}^{s,z}\} \Rightarrow$  compute  $\{\hat{E}_t^s, \hat{C}^{s,z}\} \Rightarrow$  compute  $\{\hat{\tau}_{ijt}^s\}$ .

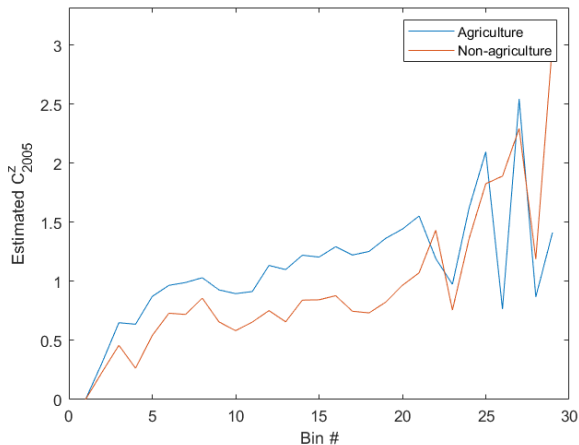
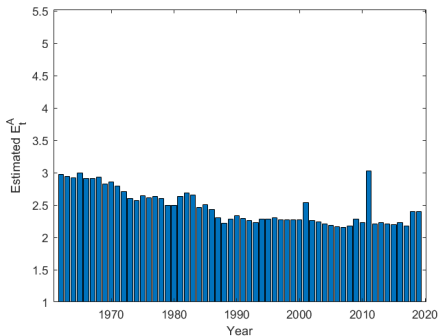


Figure: Estimated cost of distance bins ( $\hat{C}^{s,z}$ )

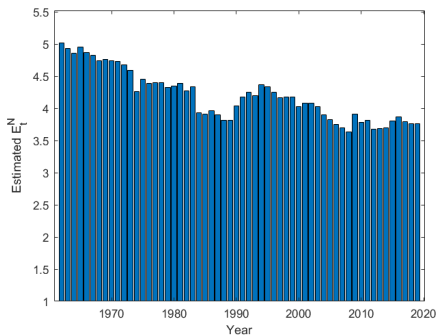
# Results: Trade Costs (2/2)

Figure: Estimated border-crossing costs ( $\hat{E}_t^s$ )

## Agriculture



## Non-Agriculture



- Substantial decline in border-crossing costs over the decades (but still high in 2019).

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# Calibrating Local Fundamentals

- We already have:
  - Estimated trade costs  $\hat{\tau}_t$  for each year  $t$ .
  - Data in year  $t$  (wages, populations, sectoral employment). Data
  - Parameter values (from literature). Parameters Normalization
- Given these inputs, can solve system of equilibrium equations to recover fundamentals  $(\bar{A}_t^A, \bar{A}_t^N, \bar{u}_t)$  that rationalize data from year  $t$ :

$$(w_{it})^{\sigma_s} (L_{it}^s)^{1-\alpha_s(\sigma_s-1)} = \sum_{j \in \mathcal{S}} (\hat{\tau}_{ijt}^s)^{1-\sigma_s} (\bar{A}_{it}^s P_{jt}^s)^{\sigma_s-1} v_{jt}^s L_{jt} w_{jt}$$

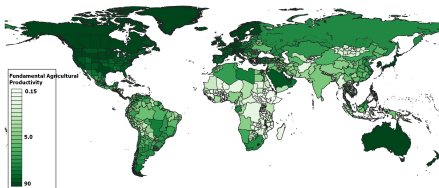
$$(P_{jt}^s)^{1-\sigma_s} = \sum_{i \in \mathcal{S}} (\hat{\tau}_{ijt}^s w_{it})^{1-\sigma_s} (\bar{A}_{it}^s (L_{it}^s)^{\alpha_s})^{\sigma_s-1}$$

$$v_{jt}^A = \phi + \nu (P_{jt}^A / P_{jt}^N)^\gamma w_{jt}^{-\eta}, \quad L_{it} = \frac{W_{it}^\theta}{\sum_{k \in \mathcal{C}} W_{kt}^\theta} \bar{L}_{c(i),t},$$

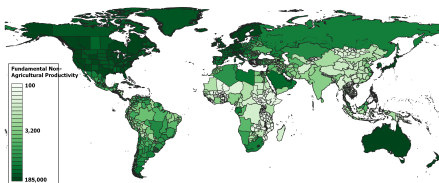
$$W_{jt} = \bar{u}_{jt} L_{jt}^\beta \left[ \frac{1}{\eta} (w_{jt} (P_{jt}^A)^{-\phi} (P_{jt}^N)^{\phi-1})^\eta - \frac{\nu}{\gamma} (P_{jt}^A / P_{jt}^N)^\gamma + \frac{\nu}{\gamma} - \frac{1}{\eta} \right]$$

# Results: Calibrated Fundamental Productivities (2005)

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## Non-Agriculture



Calibrated Fundamental Amenities

- Intuitive: high productivities in developed/oil-rich locations.

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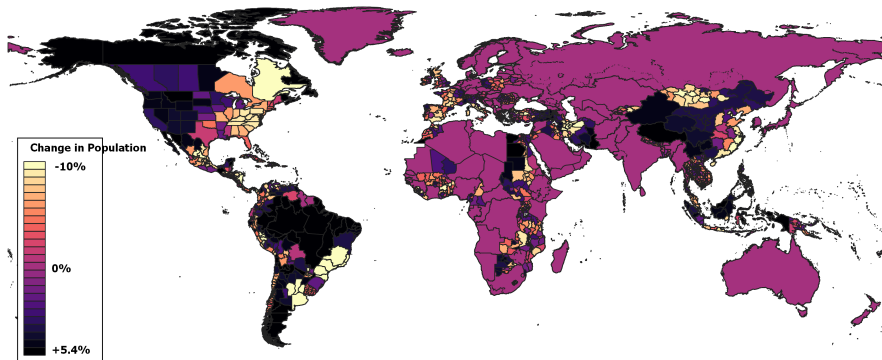
- Choose counterfactual trade-cost matrix  $\tau^{cf}$ :
  - **CF #1**: remove all border-crossing costs.
  - **CF #2**: roll back trade-cost structure to 1971.
- Given  $\tau^{cf}$  and fundamentals  $(\bar{A}_t^s, \bar{u}_t)$ , solve system of equilibrium equations (1)-(4)
  - Recover counterfactual endogenous variables (population, wage, welfare, etc).

## Equilibrium System

- **Interpretation**: how would the world economy look like if...
  - trade costs were different...
  - but the other fundamentals (productivities, amenities) remained the same as in the 2005 baseline?

# Results: Counterfactual #1 (no border-crossing costs)

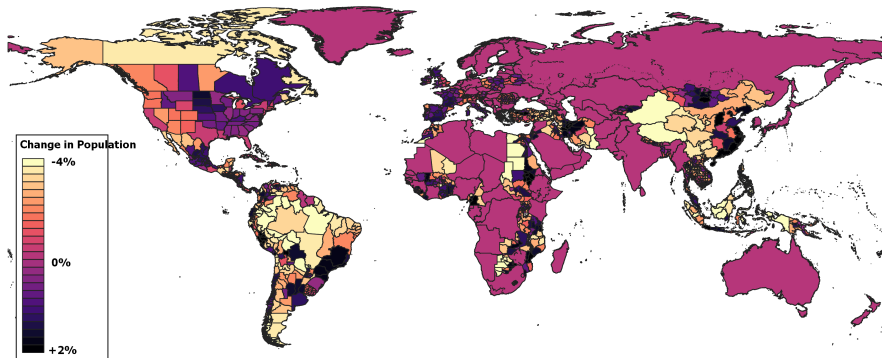
Change in Population



- Counterfactual trade costs are:  $\tau_{ij}^{s,cf} = \prod_{z=1}^B (\hat{C}^{s,z})^{\mathbb{1}_{dist_{ij} \in bz}}$
- Spatial concentration **falls**:  $\rho\left(\ln(L_{i,baseline}^{sh}), \Delta \ln(L_i)\right) = -0.227$ 
  - Initially large locations shrink.

## Results: Counterfactual #2 (1971 trade costs)

Change in Population



- Counterfactual trade costs are:  $\tau_{ij}^{S,cf} = \hat{\tau}_{ij,1971}^S$
- Spatial concentration **rises**:  $\rho\left(\ln(L_{i,baseline}^{sh}), \Delta \ln(L_i)\right) = 0.249$ 
  - Initially large locations grow.

# Results: Counterfactual Trade and Welfare

- International trade (as % of world GDP):

Scenario	CF #1	CF #2
Baseline	0.21	0.21
Long-Run CF	<b>0.78</b>	<b>0.14</b>
CF (strong immobility)	0.78	0.16
CF (weak immobility)	0.78	0.14

- Cross-country average of national welfare ( $\pi_c \equiv (\sum_{k \in c} W_k^\theta)^{\frac{1}{\theta}}$ ):

Scenario	CF #1	CF #2
Baseline	1	1
Long-Run CF	<b>1.569</b>	<b>0.949</b>
CF (strong immobility)	1.568	0.956
CF (weak immobility)	1.569	0.949

- Even from 2005 starting point, further trade integration would still yield large gains.

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- How much of observed 1990-2005 changes in concentration is accounted for by:
  - Structural transformation (**ST**)?
  - Differential trade access (**DTA**)?
  - Local fundamentals (**LF**): productivities/amenities?
- Calibrate world economy separately for 1990 and 2015.
- Then use equation (6) to separate contributions of three factors:

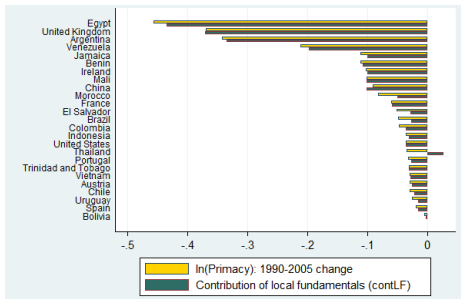
$$\ln(\text{Primacy}_{c,2005}) - \ln(\text{Primacy}_{c,1990}) = \text{contrib}_c^{ST} + \text{contrib}_c^{DTA} + \text{contrib}_c^{LF}$$

Equation: primacy rate

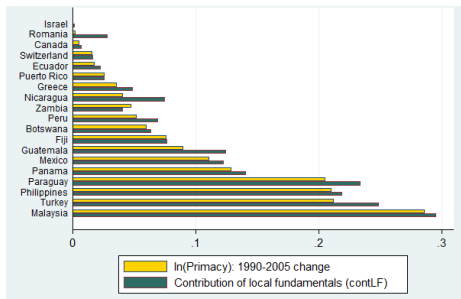
- Can also decompose cross-country variance of primacy changes ( $d \ln(\text{Primacy}_c)$ ) into sum of variances of three factors (plus bilateral covariances).

# Results: Change Accounting (1/2)

$dPrimacy_c < 0$



$dPrimacy_c > 0$



Country-by-country table

## Results: Change Accounting (2/2)

- Decomposition of  $\text{Var}(d \ln(\text{Primacy}))$ :

		in %
$\text{Var}(\text{contrib}^{ST})$	0.000002	0.008%
$\text{Var}(\text{contrib}^{DTA})$	.0002	0.99%
$\text{Var}(\text{contrib}^{LF})$	.0202	103.7%
$2\text{cov}(\text{contrib}^{ST}, \text{contrib}^{DTA})$	-0.000005	-.03%
$2\text{cov}(\text{contrib}^{ST}, \text{contrib}^{LF})$	.00005	0.25%
$2\text{cov}(\text{contrib}^{DTA}, \text{contrib}^{LF})$	-.001	-4.93%
$\text{Var}(d \ln(\text{Primacy}))$	.0195	100%

$$\begin{aligned}\text{Var}(d \ln(\text{Primacy})) &= \text{Var}(\text{contrib}^{ST}) + \text{Var}(\text{contrib}^{DTA}) + \text{Var}(\text{contrib}^{LF}) \\ &+ 2\text{cov}(\text{contrib}^{ST}, \text{contrib}^{DTA}) + 2\text{cov}(\text{contrib}^{ST}, \text{contrib}^{LF}) + 2\text{cov}(\text{contrib}^{DTA}, \text{contrib}^{LF})\end{aligned}$$

- Bottom line:** dominant influence of local fundamentals.

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- Augment a quantitative spatial model with non-homothetic preferences to study three drivers of spatial concentration:
  - Structural transformation, differential trade access, and local fundamentals.
- Bring model to the data:
  - Estimate global trade-cost structure between 1962-2019.
  - Calibrate model to the world economy in 1990 and 2005.
- Perform counterfactual exercises to assess effect of trade shocks:
  - For most countries, trade decreases concentration.
- Decompose 1990-2005 changes in concentration into roles of the three factors:
  - Local fundamentals were the dominant factor.
  - Only 1% of variance is explained by trade access.

- World is a set  $\mathcal{S}$  of locations.
  - Locations:  $i \in \mathcal{S} = \{1, \dots, N\}$ .
- World is partitioned into set of countries  $\mathcal{C}$ .
  - Countries:  $c \in \mathcal{C} = \{1, \dots, C\}$ .
  - Function  $c : \mathcal{S} \rightarrow \mathcal{C}$  maps locations to countries.
- Define the primacy function  $p : \mathcal{C} \rightarrow \mathcal{S}$ 
  - Maps each country to its largest city (primate).
  - It is an equilibrium object.
- Two sectors:
  - Agriculture ( $s = A$ ) and non-agriculture ( $s = N$ ).

## Model: Agents (1/2)

- Agent who is born in location  $i$  and moves to  $j$  receives welfare:

$$W_j(\epsilon) = \underbrace{C_j u_j}_{\equiv W_j} \epsilon_j$$

where  $C_j$  is PIGL indirect utility function (Eckert Peters '18):

$$C_j = \frac{1}{\eta} \left( \frac{w_j}{(P_j^A)^\phi (P_j^N)^{1-\phi}} \right)^\eta - \frac{\nu}{\gamma} \left( \frac{P_j^A}{P_j^N} \right)^\gamma + \frac{\nu}{\gamma} - \frac{1}{\eta}$$

- $P_j^s = (\sum_{k \in \mathcal{S}} (p_{kj}^s)^{1-\sigma_s})^{\frac{1}{1-\sigma_s}}$  is CES price index for sector  $s$ .
- $w_j$  is local wage,  $p_{kj}^s$  is local price of sector- $s$  good from  $k$ .
- Non-homothetic preferences and **structural transformation**:
  - Agricultural spending share  $v_j^A$  decreases with income.

$$v_j^A = \phi + \nu (P_j^A / P_j^N)^\gamma w_j^{-\eta}$$

## Model: Agents (2/2)

- Agent who is born in location  $i$  and moves to  $j$  receives welfare:

$$W_j(\epsilon) = \underbrace{C_j u_j}_{\equiv W_j} \epsilon_j$$

- $u_j = \bar{u}_j L_j^\beta$  is **local amenity** ( $\beta \leq 0$ ).
- $\epsilon_j$  is idiosyncratic taste shock for location  $j$ .
  - i.i.d. Fréchet distribution:  $\Pr(\epsilon_j \leq x) = \exp(-x^{-\theta})$
- Migration decision:
  - Agent born in  $i$  migrates to highest-welfare destination:

$$\max_j W_{ij}(\epsilon)$$



- Sector  $s$  in location  $i$  has continuum of perfectly competitive firms with production function:

$$q_i^s = A_i^s l_i^s, \text{ with: } A_i^s = \bar{A}_i^s (L_i^s)^{\alpha_s}$$

- $A_i^s$  is **local productivity** of sector  $s$
  - $l_i^s$  is firm employment.
  - $L_i^s$  is local employment in sector  $s$ .
  - External economies of scale ( $\alpha_s \geq 0$ ): related to NEG
- Firm sells good worldwide paying “iceberg” **shipping cost**:
    - $\tau_{ij}^s \geq 1$ , with  $\tau_{ii}^s = 1$
- Assumptions imply the pricing equation:

$$p_{ij}^s = \frac{\tau_{ij}^s w_i}{A_i^s} \quad (8)$$

- Bilateral trade flows ( $X_{ij}^s$ ) assume “gravity” form:

$$X_{ij}^s = \left[ \frac{\tau_{ij}^s w_i}{A_i^s P_j^s} \right]^{1-\sigma_s} v_j^s w_j L_j \quad (9)$$

where  $L_j$  is local population and  $v_j^N = 1 - v_j^A$ .

- So do bilateral migration flows ( $L_{ij}$ ):

$$L_{ij} = \left( \frac{(W_j)^\theta}{\sum_{k \in \mathcal{S}} (W_k)^\theta} \right) L_i \quad (10)$$

# Model: Equilibrium Conditions

- **(I)** Goods markets clear:

$$w_i L_i^s = \sum_{j \in \mathcal{S}} X_{ij}^s, \quad \forall (i, s) \quad (11)$$

- **(II)** Local labor markets clear:

$$L_i = \sum_{j \in \mathcal{S}} L_{ij} = \sum_{j \in \mathcal{S}} L_{ji}, \quad \forall i \quad (12)$$

- Like steady-state of dynamic spatial migration model

- **(III)** Local population adds up:

$$L_i = L_i^A + L_i^N, \quad \forall i \quad (13)$$

- **(IV)** National population adds up:

$$\bar{L}_c = \sum_{i \in \mathcal{C}} L_i, \quad \forall c \in \mathcal{C} \quad (14)$$

# Microfoundation: Trade Costs

- Path from  $i$  to  $j$ , partitioned into  $B$  segments with lengths  $\{dx_b\}_{b=1}^B$ .
- The final amount of goods is approximately given by:

$$q_f \approx q_0 \prod_{k=1}^B r(x_k)^{\frac{dx_k}{s(x_k)}} \quad (15)$$

- $x_k$ : arbitrarily chosen point in segment  $k$ .
  - $r(x)$ : “Net-of-melting” rate (per unit of time).
  - $s(x)$ : speed.
- Take limit: infinitesimal partitioning yields iceberg trade cost:

$$\tau_{ij} = \frac{q_0}{q_f} = \lim_{dx \rightarrow 0} \prod_{k=1}^B \left( r(x_k)^{\frac{1}{s(x_k)}} \right)^{dx_k} = \pi_i^j \left( r(x)^{\frac{1}{s(x)}} \right)^{dx} \quad (16)$$

where  $\pi$  indicates the geometric integral.

- By properties of geometric integral:

$$\tau_{ij} = e^{\int_i^j \ln(r(x)^{\frac{1}{s(x)}}) dx} = e^{\int_i^j \frac{1}{s(x)} \ln(r(x)) dx}$$

# Calibration of Modal Traversal Costs

- Consider trade costs  $T(i, j)$  in Allen Arkolakis '14, assuming:
  - $\theta = 1$
  - A single model of transportation  $m$
  - No fixed cost ( $b_m = 0$ )
- Yields:  $T(i, j) = e^{a_m d_m(i, j)}$
- Distance  $d_m(i, j)$  can be represented as  $\int_i^j \tau_{mode}(x) dx$ 
  - $\tau_{mode}(x)$ : relative “slowness” of mode  $m$
- Matching terms in integral  $e^{\int_i^j \frac{1}{s(x)} \ln(r(x)) dx}$ , obtain:

$$a_m \tau_{mode}(x) = \frac{1}{s(x)} \ln(r(x)) \quad (17)$$

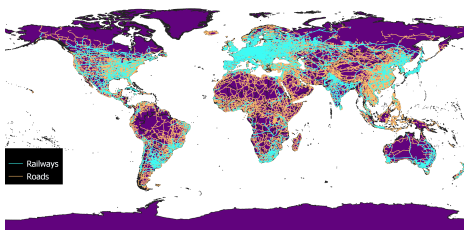
- Therefore, can calibrate by using:
  - $a_m$  from Row 1, Table II
  - $\tau_{mode}(x)$  from Appendix B3

# Measuring Distances (1/2)

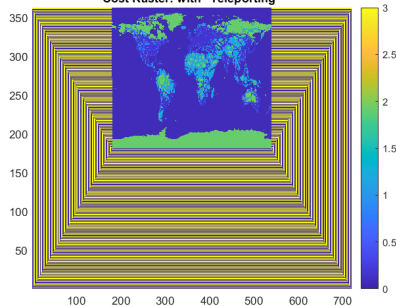
- Bilateral distances ( $dist_{ij}$ ) are key inputs for gravity estimation.
  - How do we measure them?
- Generate *cost raster* using infrastructure network maps:
  - Assign traversal cost  $T(x)$  to each  $1^\circ$ -by- $1^\circ$  pixel  $x$ .
  - Mode-specific traversal costs adapted from Allen Arkolakis '14.

Details

Global Transportation Infrastructure



Cost Raster: with "Teleporting"



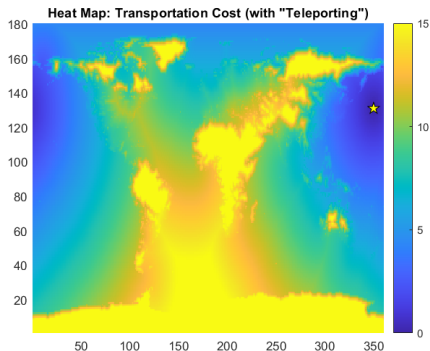
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## Measuring Distances (2/2)

- Define  $\mathcal{P}_{ij}$  as set of continuous paths  $\mathbb{P}$  on world map starting at pixel  $i$  and ending at  $j$ . Then:

$$dist_{ij} = \min_{\mathbb{P} \in \mathcal{P}_{ij}} \sum_{x \in \mathbb{P}} T(x)$$

- How to solve minimization?
  - Use FMM algorithm
  - (from Allen Arkolakis '14)



## Data Sources (1/2)

- IPUMS International: location-level population, sectoral employment.
  - Harmonized censuses (88 countries, 1605 locations).
  - Locations are typically states or provinces.
  - Covers 1960-2015 period.
  - Use year closest to 2005 (or 1990).
- World Bank Open Data:
  - Country-level data.
  - Population, GDP per capita, agricultural employment share.
  - Covers 1960-2017 period.
- G-Econ 4.0: income per capita (Desmet et al '18)
  - Data at  $1^\circ \times 1^\circ$  grid-cell level.
  - Proxy for wages.
  - Covers 1990, 1995, 2000, 2005.



## Data Sources (2/2)

- WITS: World Integrated Trade Solutions data set.
  - Country-level bilateral trade flows (total and in agriculture).
  - Covers 1962-2019 period, 222 countries.
  - But no intranational flows ( $X_{nn}^s$ ):
    - Augment data using import share and agricultural share of GDP (World Bank Open Data).
- IPUMS maps: geographic coordinates
  - Polygon's centroids.
- Natural Earth: global transportation infrastructure (Desmet et al '18)
  - Maps: roads, railway lines, oceans, landmasses.
- Final calibration sample (2005):
  - 1611 locations across 192 countries.

Data Adjustments

- Scale local IPUMS populations to match national WBOD population:

$$L_{i,2005}^s = L_{i,2005}^{s,IPUMS} \frac{\bar{L}_{c(i),2005}^{WBOD}}{\sum_{j \in c(i)} L_{j,2005}^{IPUMS}}$$

- Impute locations' wages using per capita income data from G-Econ:

$$w_{i,2005} = \sum_{g=1}^G \text{wagecell}_{g,2005}^{G-Econ} \left( \frac{\text{Area}_{g \cap i}}{\text{Area}_i} \right)$$

## Data Adjustments (2/2)

- To obtain intranational trade flows ( $X_{ii,t}^s$ ):

- Use WITS data to obtain country-year sectoral exports and country-year imports:

$$EXP_{it}^s = \sum_{j \neq i} X_{ijt}^{s,WITS}, \quad IMP_{it} = \sum_{j \neq i} (X_{jit}^{A,WITS} + X_{jit}^{N,WITS})$$

- Use country-year imports and import share to compute implied GDP

$$Y_{it} = \frac{IMP_{it}}{Msh_{it}}$$

- Divide GDP between sectors using agricultural share of GDP:

$$Y_{it}^A = Y_{it} \times Agsh_{it}, \quad Y_{it}^N = Y_{it} \times (1 - Agsh_{it})$$

- Subtract sectoral exports from sectoral GDP:

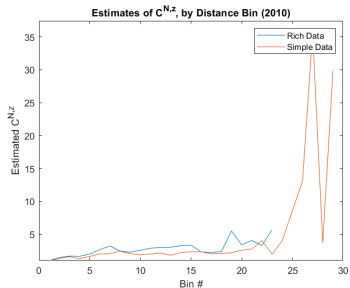
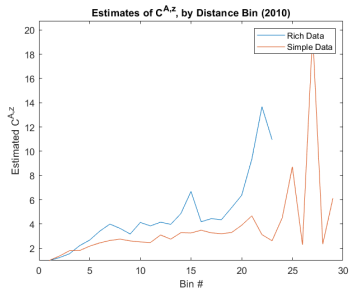
$$X_{iit}^s = Y_{it}^s - EXP_{it}^s$$

# Robustness of Trade Cost Results (1/2)

- German Survey *Verkehrsvflechtungsprognose 2030* (GSV)
  - 265 regions in 24 European countries, plus 16 non-European countries.
  - Includes intranational trade flows (helps identify border-crossing cost).
  - 15 sectors, aggregated into agriculture vs non-agriculture.
  - Richer than WITS but covers 2010 only.
- Rerun gravity regressions with GSV (for 2010 only):
  - Compare results to WITS'.
  - If they are similar, that is reassuring.
- Adjust GSV so that country-level flows match WITS:

$$X_{ij}^{s,GSV_1} = X_{ij}^{s,GSV_0} \frac{X_{c(i),c(j)}^{s,WITS}}{\sum_{i \in c(i)} \sum_{j \in c(j)} X_{ij}^{s,GSV_0}}$$

# Robustness of Trade Cost Results (2/2)



Estimate: Border-Crossing Parameters (2010)

	"Rich"		"Simple"	
	(1)	(2)	(3)	(4)
$\hat{E}_{2010}^A$	1.871		2.39	
$\hat{E}_{2010}^N$		3.73		3.81
N	32,483	34,165	18,357	18,394
WITS?	Yes	Yes	No	No
GSV?	No	No	Yes	Yes

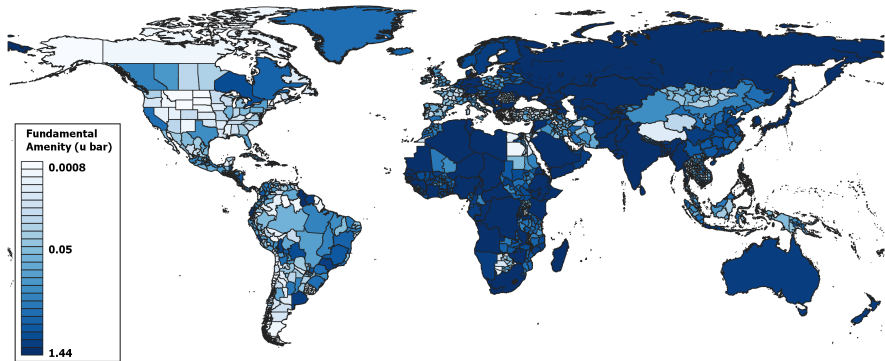
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- Parameter values taken from the literature:

Parameter	Description	Value
$\sigma_A, \sigma_N$	Elasticities of substitution	4
$\theta$	Dispersion of taste shock	1.2
$\alpha_A, \alpha_N$	Agglomeration elasticities	0.1
$\beta$	Congestion elasticity	-0.345
$\phi$	Asymptotic agricultural share of consumption	0.01
$\nu$	Degree of non-homotheticity	0.5
$\gamma$	Concavity of non-homothetic part of utility	0.35
$\eta$	Concavity of Cobb-Douglas part of utility	0.31

- Normalization:**  $\pi_c \equiv \left( \sum_{k \in \mathcal{C}} W_{kt}^\theta \right)^{\frac{1}{\theta}} = 1$  for all countries  $c \in \mathcal{C}$ 
  - Reason: country's average welfare levels and amenity levels not separately identifiable.

# Results: Calibrated Fundamental Amenities (2005)



Back

- Given counterfactual equilibrium allocation, recover counterfactual variables of interest:
  - Country's primacy rate and average welfare:

$$Primacy_c^{cf} = L_{p_{cf}(c)}^{cf} / \bar{L}_c$$

$$\pi_c^{cf} = \left( \sum_{k \in c} (W_k^{cf})^\theta \right)^{\frac{1}{\theta}}$$

- International trade (as % of world GDP):

$$\left( \frac{M}{Y} \right)^{cf} = \frac{\sum_{s \in \{A, N\}} \sum_{i \in S} \sum_{j \notin c(i)} X_{ij}^{s, cf}}{\sum_{s \in \{A, N\}} \sum_{i \in S} \sum_{j \in S} X_{ij}^{s, cf}}$$

- Effect of on variable  $y$  obtained by comparing  $y^{cf}$  to  $y_t$ .



## Counterfactuals With Immobility (1/2)

- How much does worker spatial/sectoral reallocation influence the effects of trade shocks on welfare and trade volume?
- Compare long-run counterfactual to “immobility” counterfactuals:
  - **Strong** immobility: no reallocation across sectors or locations.
  - **Weak** immobility: reallocation across sectors but not locations.
- *Strong*: solve system for  $(w^{cf,Sl,s}, P^{cf,Sl,s}, v^{cf,Sl,s \times s'})$ :

$$(w_i^{cf,Sl,s})^{\sigma_s} (L_{i,2005}^s)^{1-\alpha_s(\sigma_s-1)} = (\bar{A}_{i,2005}^s)^{\sigma_s-1} \sum_{j \in S} (\tau_{ij}^{cf,s})^{1-\sigma_s} (P_j^{cf,Sl,s})^{\sigma_s-1} \sum_{r \in \{A,N\}} v_j^{cf,Sl,s \times r} L_{j,2005}^r w_j^{cf,Sl,r}$$
$$(P_j^{cf,Sl,s})^{1-\sigma_s} = \sum_{i \in S} (\hat{\tau}_{ij,2005}^s w_i^{cf,Sl,s})^{1-\sigma_s} (\bar{A}_{i,2005}^s (L_{i,2005}^s)^{\alpha_s})^{\sigma_s-1}$$
$$v_j^{cf,Sl,A \times s} = \phi + \nu (P_j^{cf,Sl,A} / P_j^{cf,Sl,N})^\gamma (w_j^{cf,Sl,s})^{-\eta}$$

## Counterfactuals With Immobility (2/2)

- Weak: solve system for  $(w^{cf,WI}, L^{cf,WI,s}, P^{cf,WI,s}, v^{cf,WI,s})$ :

$$(w_i^{cf,WI})^{\sigma_s} (L_i^{cf,WI,s})^{1-\alpha_s(\sigma_s-1)} = (\bar{A}_{i,2005}^s)^{\sigma_s-1} \sum_{j \in \mathcal{S}} (\tau_{ij}^{cf,s})^{1-\sigma_s} (P_j^{cf,WI,s})^{\sigma_s-1} v_j^{cf,WI,s} L_{j,2005} w_j^{cf,WI}$$

$$(P_j^{cf,WI,s})^{1-\sigma_s} = \sum_{i \in \mathcal{S}} (\tau_{ij}^{cf,s} w_i^{cf,WI})^{1-\sigma_s} (\bar{A}_{i,2005}^s (L_i^{cf,WI,s})^{\alpha_s})^{\sigma_s-1}$$

$$v_j^{cf,WI,A} = \phi + \nu (P_j^{cf,WI,A} / P_j^{cf,WI,N})^\gamma (w_j^{cf,WI})^{-\eta}$$

$$L_{i,2005} = L_i^{cf,WI,A} + L_i^{cf,WI,N}$$

## Results: Counterfactuals With Immobility

- International trade (as % of world GDP):

Counterfactual #	CF1	CF2
Baseline	0.21	0.21
Long-Run CF	0.78	0.14
CF (strong immobility)	0.78	0.16
CF (weak immobility)	0.78	0.14

- Cross-country average of national welfare ( $\pi_c \equiv (\sum_{k \in c} W_k^\theta)^{\frac{1}{\theta}}$ ):

Counterfactual #	CF1	CF2
Baseline	1	1
Long-RUn CF	1.569	0.949
CF (strong immobility)	1.568	0.956
CF (weak immobility)	1.569	0.949

- Welfare/trade volumes in immobility CFs similar to long-run CF.
  - Worker sectoral/spatial mobility are secondary factors mediating trade-shock effects on welfare/trade volumes.

## Results: Change Accounting, country-by-country (1/2)

Country	$Primacy_{c,2005}$	$d \ln(Primacy_c)$	$cont_c^{ST}$	$cont_c^{DTA}$	$cont_c^{LF}$
Argentina	0.371	-0.342	0.000	-0.008	-0.334
Austria	0.203	-0.029	-0.000	-0.003	-0.026
Bolivia	0.295	-0.005	0.000	-0.003	-0.002
Botswana	0.193	0.060	-0.000	-0.003	0.064
Brazil	0.227	-0.049	-0.000	-0.022	-0.027
Canada	0.384	0.005	-0.000	-0.002	0.007
Chile	0.345	-0.029	-0.000	-0.007	-0.022
China	0.092	-0.091	-0.000	0.011	-0.101
Colombia	0.229	-0.048	0.000	-0.012	-0.036
Benin	0.112	-0.111	-0.000	-0.003	-0.108
Ecuador	0.649	0.018	-0.000	-0.005	0.023
El Salvador	0.332	-0.052	0.000	-0.024	-0.028
Fiji	0.427	0.076	-0.000	-0.001	0.077
France	0.206	-0.061	0.000	-0.002	-0.059
Greece	0.268	0.036	0.001	-0.014	0.049
Guatemala	0.291	0.090	-0.000	-0.035	0.125
Indonesia	0.201	-0.037	0.001	-0.006	-0.032
Ireland	0.288	-0.103	0.000	-0.003	-0.100
Israel	0.242	0.000	0.000	-0.001	0.001
Jamaica	0.230	-0.112	0.000	-0.012	-0.100
Malaysia	0.284	0.286	-0.000	-0.009	0.296
Mali	0.182	-0.101	0.001	-0.000	-0.102
Mexico	0.138	0.111	-0.001	-0.011	0.123

## Results: Change Accounting, country-by-country (2/2)

Country	$Primacy_{c,2005}$	$d \ln(Primacy_c)$	$cont_c^{ST}$	$cont_c^{DTA}$	$cont_c^{LF}$
Morocco	0.130	-0.082	-0.000	-0.032	-0.050
Nicaragua	0.330	0.041	-0.000	-0.035	0.075
Panama	0.567	0.129	0.000	-0.012	0.141
Paraguay	0.279	0.205	0.000	-0.029	0.234
Peru	0.355	0.052	0.000	-0.017	0.069
Philippines	0.054	0.210	0.008	-0.016	0.219
Portugal	0.203	-0.032	0.000	-0.005	-0.027
Puerto Rico	0.728	0.026	0.000	0.000	0.026
Romania	0.094	0.003	0.001	-0.027	0.028
Vietnam	0.107	-0.030	0.000	-0.002	-0.028
Spain	0.173	-0.020	0.000	-0.005	-0.015
Switzerland	0.184	0.016	0.000	-0.001	0.017
Thailand	0.090	-0.034	0.001	-0.062	0.027
Trinidad and Tobago	0.875	-0.031	0.000	0.001	-0.031
Turkey	0.186	0.212	0.000	-0.037	0.249
Egypt	0.198	-0.456	0.000	-0.022	-0.434
United Kingdom	0.144	-0.369	0.000	0.000	-0.370
United States	0.117	-0.037	-0.000	0.000	-0.037
Uruguay	0.455	-0.026	-0.000	-0.010	-0.015
Venezuela	0.120	-0.212	0.002	-0.016	-0.198
Zambia	0.304	0.047	0.000	0.006	0.041

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